Supporting Information to

Shape-Dependent Multi-Exciton Emission and Whispering Gallery Modes in Supraparticles of CdSe/Multi-Shell Quantum Dots

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Synthesis of core/multi-shell quantum dots

All QD syntheses were performed in a nitrogen atmosphere and stored in a glovebox and with pre-dried chemicals.

Chemicals. Cd(Ac)₂ (Sigma-Aldrich, 99%), diethylzinc (Et₂Zn, Sigma-Aldrich, 1.0 M solution in hexane), Oleic acid (OA, Sigma-Aldrich, 90%), octadecene (ODE, Sigma-Aldrich, 90%), octadecene amine (ODA, Sigma-Aldrich, 90%) selenium (Strem Chemicals, 99.99%), sulphur (Alfa Aesar, 99%), trioctylphosphine (TOP, Sigma-Aldrich, 90%), trioctylphosphine oxide (TOPO, Sigma-Aldrich, 99%), were used for the synthesis of nanoparticles (NPs).

Solvents. Acetone (Merck), cyclohexane (Sigma-Aldrich, anhydrous, 99%), hexane (Sigma-Aldrich, anhydrous, 99.8%), methanol (Sigma-Aldrich, anhydrous, 99.8%), toluene (Sigma-Aldrich, anhydrous, 99.8%)

Synthesis of CdSe nanocrystal seeds. Following Ref. 1. Prior to the synthesis of the CdSe quantum dots 2 precursors were synthesized. OA (3.68 g), ODE (25.92 g), and Cd(Ac)₂ (0.64 g) were mixed, heated to 150°C, and kept under vacuum for 2 h to form Cd(OA)₂. Selenium (4.25 g) was dissolved in TOP (22.5 g) at 50°C, followed by the addition of ODE (35.7 g).

CdSe nanocrystal seeds were synthesized in 50 ml three-neck flask using a Schlenk-line. TOPO (1.11 g), ODA (3.20 g), and Cd(OA)₂-precursor (4.9 g) were mixed, heated to 300°C. When this temperature was reached the Se-precursor (5.2 g) was added rapidly. The size of the quantum dots can be tuned via changing the reaction time. The particles were diluted by adding 1 equivalent of hexane. The quantum dots were washed by adding 2 equivalents of methanol and collecting the upper hexane layer (coloured) and add 1 equivalent of acetone to precipitate the QDs. Finally, the nanocrystal seeds were re-dissolved in toluene and stored inside a glove box under nitrogen atmosphere.

Typical synthesis of CdSe/CdS/CdZnS/ZnS nanocrystals. Prior to the synthesis of the CdSe quantum dots three precursors were prepared. The zinc precursor solution (0.1 M) was

prepared by dissolving Zn(Et)₂ (0.494 g) in oleic acid (5.05 mL) and ODE (19.8 mL) at 310 °C. The cadmium precursor solution (0.1 M) was prepared by dissolving Cd(Ac)₂ (1.10 g) in oleic acid (10.83 g) and ODE (43.20 mL) at 120°C under vacuum for 2 hours. The sulphur precursor solution (0.1 M) was prepared by dissolving sulphur (0.032 g) in ODE (10 mL) at 180 °C. The Cd-, Zn-, and Cd/Zn-precursor solutions were kept at about 80 °C, while the sulphur injection solution was allowed to cool to room temperature. For each shell growth, a calculated amount of a given precursor solution was injected with a syringe using standard air-free procedures. CdSe QDs (1·10⁻⁷M of 2.91 nm QDs), ODE (5.0 g) and ODA (1.5 g) were combined and heated up to 150 °C for 1 h to remove all toluene. The reaction temperature was increased to 240 °C and in steps with reaction periods of 30 minutes the precursors were added slowly to grow the cell half-monolayer by half-layer.

Step	Total # monolayers	Added Precursors	Amount (µL)
1	0.5	Cd+S	130
2	1	Cd+S	165
3	1.5	Cd+S	205
4	2	Cd+S	250
5	2.5	Cd+S	295
6	3	Cd+S	350
7	3.5	Cd+S	410
8	4	Cd+S	470
9	4.5	Cd+S	540
10	5	Cd+S	610
11	5.5	CdZn+S	690
12	6	CdZn+S	770
13	6.5	Zn+S	855
14	7	Zn+S	940

Afterwards the reaction mixture was cooled to room temperature and diluted by adding 1 equivalent of hexane. The quantum dots were washed by adding 2 equivalents of methanol and collecting the upper hexane layer (coloured) and add 1 equivalent of acetone to precipitate the QDs. Finally, the nanocrystal seeds were re-dissolved in cyclohexane and stored inside a glove box under nitrogen atmosphere.

Determination of quantum yield of multi-shell quantum dots and supraparticles



Figure S1. Integrating sphere photon emission spectra of multi-shell quantum dot and supraball dispersions. (a) Emission spectra of the quantum dot solution in cyclohexane (red line) in a capillary, and pure cyclohexane (black line) as a reference. (b) Emission spectra of the dispersion of supraballs in water (red line) in a capillary, and pure water (black line) as a reference. From these measurements we determined the quantum yields as:

$$QY = \frac{\int_{430}^{800} \text{Phot. count}_{\text{sample}} d\lambda - \int_{550}^{800} \text{Phot. count}_{\text{ref}} d\lambda}{\int_{430}^{550} \text{Phot. count}_{\text{ref}} d\lambda - \int_{430}^{480} \text{Phot. count}_{\text{sample}} d\lambda} *100$$

Evolution of the optical resonances from core-only to core multishell nanocrystals



Figure S2. Determination and assignment of transition energies of core-only and core/ multi-shell quantum dots. (a) Low excitation intensity PL (left axis, red line) and absorption (right axis, blue line) spectra of the CdSe core-only quantum dots. (b) Assignment of the transitions in the second derivative of the absorption spectrum shown in **a**. (c) Comparison of the determined transition energies of our CdSe core only (first column) and multi-shell (last column) quantum dots with those extracted from absorption spectra taken during the incremental CdS monolayer shelling of a similarly sized CdSe core published by Van Embden *et al.* [2] As can be seen, the largest transition energy (red)shift of 190 meV occurs upon the application of the first monolayer of CdS. Subsequent addition of the second CdS monolayer already yields a much smaller redshift of 40 meV and the fourth monolayer yields only a redshift of 7 meV. In any case, the energetic position of the lowest energy absorption peak of the multishelled nanocrystals gives a good indication of the total shift of the core levels which can thus be assigned to the $1S_{3/2}1S_e$, $2S_{3/2}1S_e$, $1S_{1/2}1S_e$ and $1P_{3/2}1P_e$ levels in the multi-shell quantum dots.

The power dependence of multi-exciton emission



Figure S3. Rate equation modeling of multi-exciton populations. (a) We employ a four-level rate equation model to simulate the consecutive population of multi-exciton states. The system is pumped from the ground state G to higher states X (single exciton), X_2 (biexciton) and X_3 (triexciton) at a rate P (non-resonant absorption followed by carrier cooling). The excited states X, X₂ and X₃ decay at rates k_1 , k_2 and k_3 , respectively. We use values of $k_1 = 1/20$ ns, $k_2 = 1/1$ ns and $k_3 = 1/500$ ps [3,4]. We model the experiment with 10 ns pulses with a time-dependent pump rate of $P(t) = J\sigma/Thv$ (with *J* the fluence, $\sigma = 5 \times 10^{-15}$ cm² the absorption cross-section of the QDs, T = 5 ns the pulse duration, and hv = 3.56 eV the photon energy) if t < 5 ns, and P(t) = 0if t > 5 ns. (**b**) The evolution of the population of multi-exciton states simulated for a fluence of *J* = 10^{-3} J/cm². They reach a steady state within 5 ns. (c) The simulated emission intensity from each of the three states as a function of excitation power: $I_i = \eta_i k_i \int N_i(t) dt$, where I_i , η_i , k_i and N_i are the emission, the quantum efficiency, the decay rate, and the population of level i, respectively. We assume that for the bright fraction of QDs in the ensemble $\eta_1 = 1$, $\eta_2 = 0.1$ and $\eta_3 = 0.01$. The resulting slopes in the log-log plot are not constant, but depend on the fluence. If we nevertheless fit a single power exponent to the data points between 10⁻² and 5×10⁻² photons / QD / pulse, we obtain values well below the naively expected powers of 2 and 3 for biexciton and triexciton emission (namely, 1.6 and 1.1).

Chemical mapping of the multi-shell quantum dots using STEM-EDS



Figure S4. Chemical mapping of the multi-shell quantum dots. (**a**) HAADF-STEM image (high angle annular dark field scanning transmission electron microscopy) of several individual quantum dots. (**b**–**d**) Quantified STEM-EDS chemical maps for the elements (**b**) S, (**c**) Se, and (**d**) Zn. (**e**) Overlay image of panels **b**–**d**.

References

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